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2 **Automated Intersection Control: Performance of a Future Innovation Versus**
3 **Current Traffic Signal Control**
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1 ABSTRACT

2 Congestion is one of the biggest challenges faced by the transportation community, accounting for an
3 estimated 87.2 billion dollars in losses in 2007 alone. As such, transportation professionals need to go
4 beyond capacity expansion projects and explore novel strategies to mitigate traffic congestion. One such
5 novel strategy, automated intersection management, has been identified with the potential to greatly
6 reduce intersection delay and improve safety. While the implementation of such a system is contingent on
7 the development of automated vehicles, competitions such as DARPA's Grand and Urban Challenges
8 have shown that this technology is feasible and will be available in the future. As such, it becomes critical
9 to develop the infrastructure and associated control methods required to fully exploit the benefits of such
10 technology at the system level. This research explores one such innovative strategy, an Automated
11 Intersection Control protocol based on a First Come First Serve (FCFS) reservation system. In particular,
12 it's shown that the FCFS reservation system can significantly reduce intersection delay by exploiting the
13 features of autonomous vehicles. We present microscopic simulation experimental results and show that
14 the FCFS reservation system significantly outperforms a traditional traffic signal in reducing delay.
15

1. INTRODUCTION

As population growth has been unmatched by transportation systems' ability to handle increased levels of demand, congestion has become one of the most challenging engineering issues today. The roadway system is not only a source of mobility to drivers, but also to goods and services, and as such, the ability for this system to handle vehicle demand is paramount to the economic development of the country. Traffic congestion accounted for an estimated 87.2 billion dollars in 2007 (1), and as the ability to build excess capacity has decreased, transportation professionals have been forced to look beyond capacity expansion-based approaches to address the issue of congestion.

Federal Highway Administration's (FHWA's) Exploratory Advanced Research (EAR) Program was established by the Safe, Accountable, Flexible, Efficient Transportation Equity Act – A Legacy for Users (SAFETEA-LU). The program focuses on long-term, high-risk research “with the potential for transformational improvements to plan, build, renew, and operate safe, congestion free, and environmentally sound transportation systems.” The EAR Program addresses underlying gaps faced by applied highway research programs (www.fhwa.dot.gov/advancedresearch), anticipates emerging issues with national implications, and reflects broad transportation industry goals and objectives.

One of the EAR projects being conducted is examining the feasibility of autonomous vehicles and intersections for the future. Research in the field of artificial intelligence and robotics in recent years has made the feasibility of automated vehicles a much more tangible reality than in the past. Although the technology may not be at a stage warranting mass deployment of such vehicles in the present, it is clear that this technology has the potential to eventually become the standard. As such, it becomes important to begin to examine the consequences of what could amount to be a major overhaul of traditional operational systems as the component of automation is introduced. As congestion mitigation is an important societal problem, the operational efficiency derived from implementations aimed at exploiting the technological advantages of these automated vehicles warrants serious consideration.

Human error accounts for a majority of vehicle crashes, and prevention of these crashes through automated driving is achievable but requires new systems to coordinate the movement of autonomous vehicles in complex traffic situations. This paper evaluates an automated intersection control mechanism called First Come First Serve (FCFS) protocol developed by Dresner and Stone (2). FCFS promises to process traffic much more efficiently than traffic signals without compromising safety. Its development is guided by a set of criteria that includes the use of sensor technologies, the adoption of a standardized communication protocol, and the ability to deploy incrementally, allowing expansion to other intersections and adaptation to increasing numbers of autonomous vehicles. Absolute collision prevention, even under conditions of communications failure, is the primary goal for the system.

While that previous work introduced the FCFS protocol and demonstrated its promise as a future intersection control mechanism, all of the testing was done against ad-hoc signal timing and phasing plans. In addition to describing some refinements to the simulator and protocol, the main contribution of this paper is to validate it against traffic signals that were optimized using a software package called SYNCHRO, which is generally accepted by the transportation community. Results further confirm the promise of the FCFS protocol.

2. BACKGROUND

This section provides an overview of information relevant to this research: autonomous vehicles and their technological feasibility, and the current state of technology; current practices in traditional traffic signal design and optimization; automated intersection control and its potential benefits as an operational strategy; and microscopic simulation software and its role in numerical testing of operational strategies.

2.1 Autonomous Vehicles

The engineering challenges regarding reliable computerized control of vehicles are well understood and mostly solved for perceptually “simple” situations. Vehicles can already be equipped with features of autonomy such as adaptive cruise control, GPS-based route planning (3,4) and autonomous steering (5,6). Since the late 90s, adaptive cruise control systems have become widely available as optional equipment

1 on luxury production vehicles of most of the major car manufacturers. Early adaptive cruise control
2 systems can only slow down the vehicle when it is too close to the vehicle in front of it. But the capability
3 of adaptive cruise control systems has greatly improved since then: for instance, the adaptive cruise
4 control systems on Mercedes-Benz S-Class and GM's Cadillac SLR can automatically maintain a safe
5 following distance. Automatic parking is another autonomous feature that have already been
6 commercialized. Today's automatic parking systems such as those in Toyota Prius and BMW can
7 perform autonomous parallel parking with little or no human intervention. Other new autonomous
8 features currently offered by some car manufacturers are traffic sign recognition and lane departure
9 warning systems.

10 Building a *fully* autonomous vehicle, however, is a challenging engineering task---much more
11 difficult than adding individual features of autonomy. But there are signs that fully autonomous vehicles
12 are on the horizon. For example, in the DARPA Grand and Urban Challenges (7) in 2007, 6 autonomous
13 vehicles completed the 60 mile course of suburban-type roadways with light traffic (8). In doing so, they
14 demonstrated that it is currently possible to encode and act upon traffic laws and precisely control an
15 autonomous vehicle. In 2008, GM was experimenting with a nearly autonomous vehicle under its
16 European "Opel" brand (9). The prototype of this autonomous vehicle is called the Opel Vectra, which
17 uses a video camera, lasers, and substantial processing power to identify traffic signs, curves in the street,
18 lane markings, and other vehicles. Early this year GM demonstrated a concept vehicle EN-V that has the
19 ability to operate autonomously (10).

20 The use of autonomous vehicles has the potential to: improve safety and mobility; reduce driving
21 related stress; increase freeway capacity; reduce emissions and improve fuel efficiency. Furthermore,
22 higher expected compliance levels with traffic instructions could improve system performance.
23

24 **2.2 Traditional Traffic Signals**

25 Signal optimization methods aim to choose signal timing and phasing plans that achieve optimal values
26 for specific intersection performance metrics such as delay, throughput, queue length, etc. Intersection
27 delay, defined as the amount of time the vehicle added to a vehicle's travel time due to the presence of the
28 intersection, is the most commonly used metric for evaluating the performance of intersections. (11)

29 The operations of an intersection amount to what is a very complex system. As such, predicting
30 intersection delay exactly is often infeasible. As a result, intersection delay is usually seen as a random
31 variable. Traditional methods for estimating delay have relied on the use of analytical equations that
32 provide with point-estimates of delay, such as the expected value or specific percentiles (11). Further
33 work has been done in determining signal plans that are optimal at the network level by combining the
34 assignment and signal optimization process. A review of the area can be found in (12).

35 While signal optimization implementations have resulted in substantial operational
36 improvements, there are fundamental limitations to the operational performance of a traditional
37 intersection that stem from the need to address the safety issues arising from driving behavior, namely the
38 limited ability of drivers to process information and make subsequent decisions during the driving
39 activity.

40 As such, intersections and their associated control devices have been limited to have a simple
41 design and to minimize the number of simultaneous conflicting movements. The rules for navigating an
42 intersection consist of few elements of information, with many standard conventions limiting the number
43 of decisions the driver has to make. For example, drivers are only allowed to make left/right turns from
44 designated lanes, and are never allowed to interfere with a lane containing through traffic. Another
45 example is the use of protected left turns, which removes the need for drivers to evaluate whether gaps in
46 oncoming traffic are appropriate for make a left turn.

47 Although some measures, such as turning lane conventions, do not significantly affect
48 intersection performance, others, such as protected left turns, do significantly reduce the fraction of
49 available intersection capacity that is actually used. Like many other transportation design problems, a
50 balance must be reached between safety and operational efficiency.

1 We do make the distinction between traditional fixed time signals, which can change according to
2 the time of day, and actuated signals, in which the presence or absence of vehicles on intersection
3 approaches can affect the amount of green time for each approach in real time. This research did not
4 consider actuated signals as part of the numerical testing for this research, but will be considered as part
5 of future numerical testing.
6

7 **2.3 Autonomous Intersection Management**

8 In parallel with the development of autonomous vehicles, we consider infrastructure that is able to interact
9 with these autonomous vehicles. Among all elements in modern transportation infrastructure, intersection
10 is the most critical one that needs to be improved. Automobiles in modern urban settings spend a lot of
11 time idling at intersections, due to traffic congestion caused by inefficiency of traffic light systems and
12 stop signs, generating harmful emissions and causing an increase in fuel usage for no significant purpose.
13 According to a 2006 National Highway Traffic Safety Administration (NHTSA) report on Traffic Safety
14 Facts, intersection crashes account for about 40% of the total crashes in the US (13). In 2008, 7,772 out
15 of 37,261 fatalities on US roadways were intersection or intersection related (14). As intersections make
16 up a very small portion of the roadway, this is a wildly disproportionate amount. Furthermore, collisions
17 at intersections include significant number of side impact crashes, thus they frequently result in great
18 injury and damage.

19 Therefore, a better intersection management will be a major step towards an infrastructure for
20 fully autonomous vehicles that will revolutionize transportation of people and goods. Our research is to
21 propose a new form of intersection control can dramatically increase vehicle throughput on roads by
22 taking advantages of the capacity of autonomous vehicles.

23 The advantages of autonomous vehicle traffic are two-fold. First, the introduction of autonomous
24 drivers into intersection control allows for a greater degree of efficiency by removing the need for some
25 of the safety-oriented features of traditional intersections. The operational efficiency that can be gained
26 will be strongly influenced by the ability of the autonomous vehicle's driving mechanism to process
27 information and navigate the vehicle. As technology continues to develop, we can expect that eventually
28 autonomous vehicles will be vastly superior to human drivers in their ability to perform driving
29 operations.

30 Second, autonomous vehicles can eliminate the uncertain nature of driver behavior that influences
31 the design of intersections. In traditional intersection control, an individual driver knows what the
32 trajectory of his vehicle will be, but other drivers do not possess this information. As such drivers must
33 not only account for what they *expect* other drivers to do, but must also make decisions that are robust
34 across all potential decisions other drivers may make. For example, a driver attempting to make a non-
35 protected left turn will decide whether a gap in oncoming traffic is acceptable based not only on the
36 oncoming vehicles' current speed, but also on how the gap will change if the vehicles begin to suddenly
37 accelerate or decelerate. In the autonomous vehicle traffic, computerized drivers' decisions can be
38 communicated directly to other vehicles, or to intersection-based infrastructure. That allows for less
39 conservative driving behavior as each vehicle can more accurately predict the trajectory of other vehicles
40 in the intersection, and can in turn better predict the viability of specific movements, thus improving
41 intersection efficiency.

42 The central hypothesis of our research is that these advantages of autonomous vehicles can be
43 explored to develop an autonomous intersection control can be far superior to the traditional intersection
44 control mechanisms such as traffic signals and stop signs. In Section 2.5, we will describe our proposed
45 autonomous intersection control.
46

47 **2.4 Microscopic Simulation**

48 In order to test the performance of automated intersection control protocols, the use of microscopic
49 simulation models becomes indispensable. As the technology for autonomous vehicles is currently not at
50 the level needed for real world testing of intersections with any meaningful amount of traffic flow,

1 microscopic simulation software is necessary to obtain any estimate of the performance of systems of
2 such vehicles.

3 Microscopic simulation software packages are commonly used in the transportation field to
4 evaluate operational strategies at a very high level of resolution. Software packages such as VISSIM (15),
5 CORSIM (16) and SIMTraffic (17) can realistically simulate the vehicle-to-vehicle interactions in a
6 roadway system, and allow transportation planners to generate estimates of performance metrics such as
7 delay, throughput and travel time.

8 Despite the great value that such software packages provide, the options offered within the
9 programs are usually limited to existing transportation road elements and strategies. Furthermore, while
10 some of these software packages do provide the user with some level of access to the internal data
11 structures used for the simulation, this access is not enough to give the user the ability to incorporate the
12 intersection control system presented in this paper. For these reasons, we implemented a microsimulator
13 from scratch so as to allow the research team to model the intersection control system developed, and
14 evaluate its performance.

15 16 **2.5 The FCFS Intersection Control Protocol**

17 Current intersection control mechanisms were designed to work with human-driven vehicles only. When
18 vehicles are controlled by computers, there are opportunities to alleviate or resolve these issues by taking
19 advantage of the capabilities of autonomous vehicles, wireless communication, and smart intersection
20 management protocols. As laid out in detail in (2), an ideal autonomous intersection management
21 protocol must satisfy seven desiderata: 1) allow for fully distributed and autonomous control by the
22 driving agent, 2) have low communication complexity, 3) assume non-expensive vehicle sensors found in
23 production, 4) use a standardized communication protocol, 5) be incrementally deployable, 6) be safe, and
24 7) be efficient. Modern-day traffic signals completely satisfy all but the last one of these properties.
25 Traffic signals are very inefficient—not only do vehicles traversing intersections equipped with these
26 mechanisms experience large intersection delays, but also the intersections themselves can only manage a
27 limited traffic capacity—much less than that of the roads that feed into them. Therefore, we have
28 investigated a solution that exceeds the efficiency of traffic signals without sacrificing any of the other
29 properties.

30 31 *2.5.1 The Reservation Idea*

32 The aforementioned desiderata led to the development of an efficient intersection management system
33 developed by Dresner and Stone (2) that is a radical departure from existing traffic signal optimization
34 schemes. The solution is based on a *reservation* paradigm, in which vehicles “call ahead” to reserve
35 space-time in the intersection. The earlier a vehicle places a request, the earlier it will be granted, but
36 there is no inherent minimum or maximum lead time required for a request. In the approach, computer
37 programs denoted as *driver agents* control the vehicles, while an arbiter agent called an *intersection*
38 *manager* is assigned to each intersection. The role of the intersection manager is to grant or reject driver
39 agent requests to reserve blocks of space-time in the intersection. In brief, the paradigm proceeds as
40 follows (2):

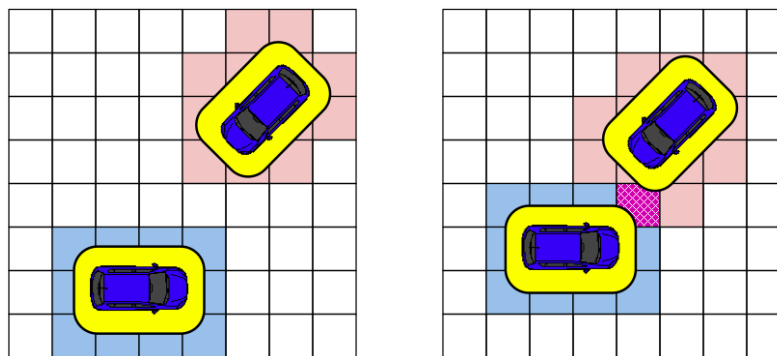
- 41
42 • An approaching vehicle announces its impending arrival to the intersection manager. The
43 vehicle indicates its predicted arrival time, arrival velocity, arrival lane and departure lanes.
- 44 • The intersection manager simulates the vehicle's path through the intersection, checking for
45 conflicts with the paths of any previously processed vehicles.
- 46 • If there are no conflicts, the intersection manager issues a reservation. It becomes the vehicle's
47 responsibility to arrive at, and travel through, the intersection as specified (within a range of error
48 tolerance).
- 49 • In the case of a conflict, the intersection manager suggests an alternate later reservation.
- 50 • The car may only enter the intersection once it has successfully obtained a reservation.

1 • Upon leaving the intersection, the car informs the intersection manager that its passage
2 through the intersection was successful.

3
4 A key feature of this paradigm is that it relies only on vehicle-to-infrastructure (V2I)
5 communication. In particular, the vehicles need not know anything about each other beyond what is
6 needed for local autonomous control (e.g., to avoid running into the car in front). While real-world
7 implementations may be subject to additional sources of error and risk, the paradigm is itself completely
8 robust to communication disruptions: if a message is dropped, either by the intersection manager or by the
9 vehicle, delays may increase, but safety is not compromised. Safety can also be guaranteed in mixed
10 mode scenarios when both autonomous and manual vehicles operate at intersections.

11 2.5.2 Intersection Control Policy

12 Our prototype intersection control policy divides the intersection into a grid of *reservation tiles*, as shown
13 in Figure 1. (This notation can be generalized for rectangular and irregularly shaped intersections.) When
14 a vehicle approaches the intersection, the intersection manager uses the data in the reservation request
15 regarding the time and velocity of arrival, vehicle size, etc. to simulate the intended journey across the
16 intersection. At each simulated time step, the policy determines which reservation tiles will be occupied
17 by the vehicle.
18
19



20
21 (a) Successful

(b) Rejected

22 **FIGURE 1 (a) The vehicle's space-time request has no conflicts at time t . (b) The vehicle's request**
23 **is rejected because at time t of its simulated trajectory, the vehicle requires a tile already reserved**
24 **by another vehicle (15)**

25 If at any time during the trajectory simulation the requesting vehicle occupies a reservation tile that is
26 already reserved by another vehicle, the policy rejects the driver's reservation request, and the intersection
27 manager communicates this to the driver agent. Otherwise, the policy accepts the reservation and reserves
28 the appropriate tiles. The intersection manager then sends a confirmation to the driver. If the reservation
29 is denied, it is the vehicle's responsibility to maintain a speed such that it can stop before the intersection.
30 Meanwhile, it can request a different reservation.

31 3. NUMERICAL TESTING: THE AIM4 SIMULATOR

32 There are many traffic simulators available for traffic purposes. Some of these simulators are designed to
33 model vehicle kinematics with extremely high fidelity, including tire friction, engine power output, and
34 even aerodynamics. Others deal with very large networks of roads or freeways, or model traffic flow
35 instead of individual vehicles (18,19). Many simulators are designed to model true human behavior,
36 rather than testing custom agent algorithms (20). When this research began, however, none gave us the
37

1 ability to easily replace the mechanism by which intersections are governed. Since this is the main focus
2 of this work, we need a custom simulator.

3 This section focuses on the features of the AIM4 simulator, with emphasis on its ability to model
4 autonomous vehicles and automated intersections.

5

6 **3.1 Vehicle Representation**

7 Each vehicle, while represented visually in the simulator as a rectangle with a fixed length and width, also
8 possesses a vector of fixed properties and a vector of state variables.

9 At a bare minimum, vehicles in the simulator have the following fixed properties: vehicle
10 identification number (VIN), length, width, front axle displacement, rear axle displacement, maximum
11 velocity, maximum acceleration, minimum acceleration, maximum steering angle, maximum steering
12 rate, sensor range, transmission range. The front and back axle displacement, which represent the distance
13 from the front of the vehicles to the front and back axle respectively, and the maximum steering rate
14 allow for more realistic limitations placed on the simulated vehicles during turning maneuvers.

15 Each vehicle also has the following state variables: position, velocity, direction, acceleration,
16 steering angle. Position is represented in a Cartesian coordinate, where the positive X-axis represents the
17 East, and the positive Y-axis represents the North. The direction in which a vehicle is facing is
18 represented as an angle, where zero radians would represent a vehicle driving east, and a vehicle with a
19 positive steering angle would be turning to the left.

20

21 **3.2 Vehicle Sensor Data**

22 As in real life, a simulated vehicle would be equipped with gauges that are designed to provide
23 information from simulated sensors that the vehicle could have. While an actual autonomous vehicle
24 would have a multitude of outward-facing sensors, including laser range finders, short-wave radar, lidar,
25 and video cameras, many of these technologies are either very difficult to simulate or do not make sense
26 in our simulated environment. We have determined that a vehicle in our simulated environment really
27 only needs to sense one thing: how far away the next vehicle in front of it is. It may not be well-defined as
28 to which vehicle is the next vehicle in front, and so we created two different sensors that try to accomplish
29 this: a simplified simulated laser range finder that can be used in any situation, and an interval sensor that
30 is much cheaper to use computationally, but can only be used when the vehicle is traveling within a lane.

31

32 *3.2.1 Simulated Laser Range Finder*

33 Simulating the complex workings of a full laser-range finder is not only computationally expensive, but
34 also more detailed than necessary for simulation purposes. Therefore, the laser range finder is
35 implemented in the simulator using a method introduced by Dresner and Stone (2). While a single sensor
36 aimed in the direction that the vehicle is moving can provide sufficient information when the vehicle is
37 driving in a straight line, it is not enough to gather enough information during a turning movement. To
38 address this, a flexible sensor is implemented in the simulator: when the vehicle is turning, the sensor's
39 range increases in the direction of the turn, while it decreases from the opposite side. This treatment of
40 sensors allows vehicles to avoid many collisions even in the absence of intersection control measures (2).
41 The main drawback of this approach is that, unamortized, it requires $O(n^2)$ distance calculations just to
42 determine which vehicles are in range of the sensor, where n is the number of vehicles.

43

44 *3.2.2 Interval Sensor*

45 The simulated laser finder is necessary in some complex driving scenarios. But in the most of the time,
46 vehicles need only know the distance the next vehicle in front of them. This can be accomplished in the
47 simulator by generating a list of vehicles and the distance from the start of the lane. While it is possible
48 for a vehicle to be in more than one lane, for example during a lane changing procedure, this can still be
49 accommodated within this system. Once each of these lists of vehicles is sorted, the distances between the
50 successive vehicles are calculated and recorded in the vehicles' interval sensor gauges. This process takes

1 only $O(n \log n)$ of computational time. Instead of only being able to simulate tens of vehicles in real time
 2 using simulated laser range finders, we can simulate hundreds using interval sensors.

3.2.3 Safety Buffers

5 The AIM4 simulator makes use of three types of buffers to protect vehicles from moving too close to each
 6 other: (i) a *static buffer* represents a constant sized space around the vehicle (e.g., 0.5m from each side of
 7 the vehicle) in which no other vehicle should present at any point in time during the traversal of the
 8 intersection; (ii) the *internal time buffer* adds additional space in the direction of travel that extends for t
 9 seconds of driving distance, thus allowing the vehicle to arrive t seconds early or late at the intersection;
 10 and (iii) the *edge time buffer* creates a time gap of t seconds at the edge of the intersection such that
 11 exiting vehicles have at least t seconds of driving distance between them, thus preventing the vehicles
 12 from exiting too close to the previous vehicle.

3.3 Communication

15 Each agent (a driver agent or an intersection manager) has two queues of messages: an *inbox* and an
 16 *outbox*. Whenever an agent wants to send a message, it places the message in its outbox. At the end of
 17 each simulation cycle, the simulator examines all agents' outboxes, takes any messages in them, and then
 18 conditionally delivers them to their destinations' inboxes. The next time the destination agents are able to
 19 act, they can examine their inboxes and take actions based on the messages present. Whether or not an
 20 individual message is delivered is a function of two things: the transmission strength of the sending agent,
 21 and the distance between the sending agent and the receiving agent. The location of an intersection, for
 22 these purposes, is the centroid of the intersection's area. For all of our experiments, we use a very simple
 23 function: the message is delivered if and only if the message strength is greater than or equal to the
 24 distance between the agents, though a stochastic model could easily be implemented.

25 One nice result of explicitly modeling communication (instead of using simple function calls, as
 26 in previous versions of the simulator) is that it allows us to do a *mixed simulation*. In a mixed simulation,
 27 one or more of the vehicles in the simulator is an actual physical vehicle. Each real vehicle corresponds
 28 to a proxy vehicle in the simulator whose state—position, velocity, and so forth—are continuously
 29 updated using data from the real vehicle. The real vehicle's sensors are fed information from the simulator
 30 to make it appear to the real vehicle that the simulated vehicles are real. This enables us to run
 31 experiments involving real vehicles without risking expensive damage to the real vehicles should
 32 something go awry (21,22).

3.4 Vehicle Controller

35 In every time step in a simulation, the AIM4 simulator updates the position, the direction, and the speed
 36 of every vehicle according to an approximate law of physics as follows. Based on some simplifying
 37 assumptions such as only planar motion is allowed and vehicles do not skid on a road, the state of a
 38 vehicle is updated using the following differential equations for non-holonomic motion:

$$\begin{aligned} \frac{\partial x}{\partial t} &= v \cdot \cos(\phi) \\ \frac{\partial y}{\partial t} &= v \cdot \sin(\phi) \\ \frac{\partial \phi}{\partial t} &= v \cdot \frac{\tan \psi}{L} \end{aligned}$$

44 where x , y , and ϕ is the coordinate and the direction of the vehicle, v is the vehicle's velocity, ψ is the
 45 steering angle, and L is the vehicle's wheelbase (i.e., the length between the front wheels and the rear
 46 wheels). Given x , y , ϕ , v , and ψ , in the previous time step, the AIM4 simulator solves these equations and

1 computes x , y , and ϕ in the next time step, assuming ψ remains constant in the time step and v changes
2 according to the acceleration a which remains constant in the time step.

3 Vehicles' controllers controls the motion of vehicles by setting the acceleration a and the steering
4 angle ψ at every time step, in the same way as drivers in the real world control vehicles by gas
5 pedal/brake and steering wheels. In the previous version of the simulator, a vehicle controller computes
6 the acceleration and the steering angle in every time step without planning ahead the entire course of
7 actions for the traversal. This can cause some difficulties in meeting the arrival time and the arrival
8 velocity requirement of the FCFS protocol (22,23). In AIM4, vehicle controllers can optionally be given
9 *acceleration schedule* and/or *track* to aide the control. An acceleration schedule is a time series of
10 accelerations: $\langle (a_1, t_1), (a_1, t_2), \dots, (a_n, t_n) \rangle$, which means that the controller should set the acceleration to a_i
11 at time t_i , for $1 \leq i \leq n$. In AIM4, when a vehicle sends a request to the intersection manager to make a
12 reservation, the vehicle controller computes an acceleration schedule such that, if follows correctly, the
13 vehicle can arrive at the intersection at the arrival time and the arrival velocity as stated in the request
14 message. The use of acceleration schedule can prevent vehicles from making reservations that are
15 impossible to keep (22,23). Likewise, a vehicle controller can control the steering angle by a given track,
16 which is usually the middle of a lane or a trajectory inside the intersection. The controller would then set
17 the steering angle so as to stay as close to the track as possible.

18 19 **3.5 The Simulation**

20 The input of the simulator consists of a map, a detailed layout of the roads and intersections, and a
21 specification of the vehicle generation at the vehicle spawn points. The simulation proceeds with a
22 sequence of time steps, each of them represents a fixed amount of time t (usually 0.02 second) in the
23 simulation. At the beginning of each time step, the simulator performs a sequence of tasks as follows:
24

25 *Task 1. Spawn Vehicles:* Vehicles are spawned according to an approximate Poisson process,
26 except when there is no room for more vehicles in the lane.

27 *Task 2. Provide Sensor Input:* For each vehicle, that vehicle's velocity, acceleration, direction,
28 and position are recorded to the speedometer, accelerometer, compass, and position gauges, respectively.
29 Additionally, the interval gauge and/or simplified laser range finder are simulated, and the results are
30 recorded to the corresponding gauges in the vehicle.

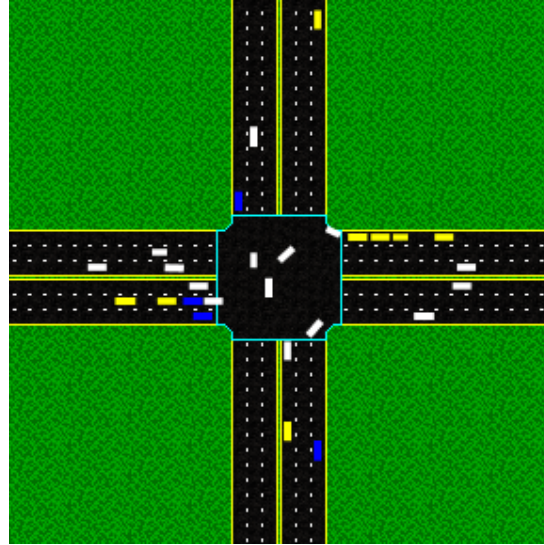
31 *Task 3. Control vehicles:* Vehicle controllers and intersection managers are given a chance to act
32 after the vehicles' sensing inputs are updated.

33 *Task 4. Deliver messages:* Any messages in the vehicles' and the intersections' outgoing
34 messages queues are delivered to their destinations.

35 *Task 5. Move Vehicles:* The positions, directions and velocities of all vehicles are updated based
36 on the physical model of the vehicles.

37 *Task 6. Clean up:* Any vehicle that has traveled outside the simulated area or has arrived at its
38 intended destination is removed from the simulation.

39
40 Figure 2 shows a screenshot of the simulator's graphical display.



1
2 **FIGURE 2 A screenshot of the simulator in action.**

3
4 **4. DESCRIPTION OF THE TESTING PROCEDURE**

5 The objective of this paper is to compare the performance of the FCFS Intersection protocol to the
6 performance of an optimized signal timing plan as generated by a standard signal optimization software
7 package. While several signal optimization software packages exist in the market, SYNCHRO (24) was
8 chosen due to the fact that it is commonly used by state agencies and private consulting agencies alike.

9 Our hypothesis is that, by significantly decreasing the amount of lost time in the intersection, the
10 intersection protocol presented in this paper will allow for much more efficient use of the time-space
11 capacity of an intersection. We will focus on the performance of both an optimized signal plan and the
12 automated intersection manager on a single, three-lane, four-approach intersection. While we realize that
13 a more varied set of scenarios is desirable, it is important to note that a validation of the model is
14 impossible for 100% of scenarios.

15 As such, we wish to establish, at least for a common intersection configuration, whether or not
16 the intersection manager outperforms a traditional intersection. Furthermore, we wish to identify what are
17 the factors that affect the potential for improvement. In particular, we will look at how performance varies
18 with changes in the total volume per approach.

19 Two general sets of scenarios will be considered:

20 i. Two Phase Intersection: 3 levels of flow for the through movement at each of the 4
21 approaches of the intersection are considered: Low (200 v/h), Medium (600 v/h), and High (1000 v/h).
22 The objective of this set of testing scenarios is to determine the effect that different combinations of
23 overall level of congestion have on the performance of the intersection. Left turn volume is kept at 100
24 v/h, and right turn volume is kept at 200 v/h.

25 ii. Three Phase Intersection with single protected Left Turn: We consider 5 levels of flow for a
26 single approach's left turning volume (200, 400, 600, 800, 1000 v/h), and 4 levels of flow for the
27 opposing approach's through movement level of flow (400, 600, 800, 1000 v/h). All other approaches
28 are kept at 500 v/h for the through movement, and 100 v/h for right and left turn movements. The objective of
29 this set of testing scenarios is to determine how the conditions of the left turning movement affect the
30 performance of the intersection.

31 For each set of testing scenarios, 4 different intersection control strategies will be tested:

- 32 i. Traditional Traffic Signal, optimized using SYNCHRO
33 ii. FCFS manager with 0.25 meter static buffer, 0.1 second internal time buffer, and 0.25 second
34 edge time buffer.

- 1 iii. FCFS manager with 0.50 meter static buffer, 0.2 second internal time buffer, and 0.50 second
- 2 edge time buffer.
- 3 iv. FCFS manager with 0.75 meter static buffer, 0.3 second internal time buffer, and 0.75 second
- 4 edge time buffer.

5
6 **5. RESULTS AND DISCUSSION**

7 The FCFS protocol significantly outperformed traditional signals in both sets of experiments conducted,
8 regardless of the traffic pattern, or selected set of safety buffers for the autonomous vehicles. Table 1
9 shows the results for the two-phase intersection experiment, and Table 2 shows the results for the Three-
10 phase intersection experiment. In each case the null hypothesis that the average from the traditional signal
11 (Y) was less than or equal to the delays of the FCFS control (X) was rejected, which allows us to
12 conclude with great confidence that the FCFS reservation system significantly outperforms a traditional
13 traffic signal in minimizing delay.

14
15 **TABLE 1 Delay for Two-phase experiment**

Flow by Approach (v/h)				Traffic Signals (Y)		FCFS (0.25,0.1,0.25)			FCFS (0.50,0.2,0.50)			FCFS (0.75,0.3,0.75)		
						(X ₂₅)			(X ₅₀)			(X ₇₅)		
EB	NB	SB	WB	average delay (s)	std dev (s)	average delay (s)	std dev (s)	H ₀ :Y-X ₂₅ ?0 H _A :Y-X ₂₅ >0	average delay (s)	std dev (s)	H ₀ :Y-X ₅₀ ?0 H _A :Y-X ₅₀ >0	average delay (s)	std dev (s)	H ₀ :Y-X ₇₅ ?0 H _A :Y-X ₇₅ >0
200	200	200	200	3.98	0.12	0.12	0.01	Reject H0	0.23	0.02	Reject H0	0.37	0.03	Reject H0
200	200	200	600	4.89	0.17	0.13	0.01	Reject H0	0.28	0.02	Reject H0	0.46	0.04	Reject H0
200	200	600	600	4.18	0.11	0.16	0.01	Reject H0	0.30	0.02	Reject H0	0.57	0.03	Reject H0
200	200	600	1000	5.86	0.18	0.29	0.02	Reject H0	0.59	0.03	Reject H0	1.24	0.12	Reject H0
200	200	1000	600	5.83	0.17	0.25	0.02	Reject H0	0.52	0.04	Reject H0	1.03	0.07	Reject H0
200	200	1000	1000	7.33	0.25	0.40	0.03	Reject H0	0.89	0.07	Reject H0	2.03	0.20	Reject H0
200	600	200	1000	5.72	0.17	0.25	0.02	Reject H0	0.53	0.04	Reject H0	1.05	0.08	Reject H0
200	600	600	200	4.66	0.20	0.15	0.01	Reject H0	0.30	0.02	Reject H0	0.53	0.04	Reject H0
200	600	600	600	4.24	0.09	0.17	0.02	Reject H0	0.35	0.02	Reject H0	0.66	0.05	Reject H0
200	600	600	1000	5.80	0.16	0.30	0.02	Reject H0	0.66	0.05	Reject H0	1.35	0.10	Reject H0
200	600	1000	200	6.15	0.18	0.23	0.02	Reject H0	0.47	0.04	Reject H0	0.91	0.07	Reject H0
200	600	1000	600	5.70	0.11	0.25	0.01	Reject H0	0.54	0.03	Reject H0	1.07	0.11	Reject H0
200	600	1000	1000	7.64	0.15	0.39	0.02	Reject H0	0.94	0.05	Reject H0	2.20	0.29	Reject H0
200	1000	200	200	6.59	0.22	0.24	0.02	Reject H0	0.46	0.04	Reject H0	0.88	0.08	Reject H0
200	1000	200	600	5.80	0.17	0.29	0.02	Reject H0	0.61	0.05	Reject H0	1.26	0.11	Reject H0
200	1000	600	200	6.06	0.14	0.23	0.02	Reject H0	0.48	0.03	Reject H0	0.88	0.07	Reject H0
200	1000	600	600	5.77	0.17	0.29	0.02	Reject H0	0.61	0.04	Reject H0	1.22	0.08	Reject H0
200	1000	600	1000	7.60	0.21	0.42	0.02	Reject H0	1.04	0.07	Reject H0	2.52	0.30	Reject H0
200	1000	1000	200	6.55	0.17	0.30	0.01	Reject H0	0.61	0.03	Reject H0	1.23	0.10	Reject H0
200	1000	1000	600	6.60	0.15	0.34	0.01	Reject H0	0.78	0.05	Reject H0	1.59	0.14	Reject H0
200	1000	1000	1000	8.56	0.19	0.50	0.03	Reject H0	1.23	0.08	Reject H0	3.06	0.31	Reject H0
600	600	600	600	4.30	0.10	0.18	0.01	Reject H0	0.39	0.03	Reject H0	0.76	0.05	Reject H0
600	600	1000	1000	6.85	0.15	0.42	0.02	Reject H0	1.04	0.08	Reject H0	2.53	0.20	Reject H0
600	1000	600	600	5.80	0.14	0.30	0.02	Reject H0	0.71	0.04	Reject H0	1.40	0.11	Reject H0
600	1000	1000	600	6.63	0.13	0.40	0.02	Reject H0	0.93	0.05	Reject H0	2.03	0.15	Reject H0
600	1000	1000	1000	8.39	0.19	0.55	0.02	Reject H0	1.39	0.10	Reject H0	3.32	0.33	Reject H0
1000	1000	1000	1000	9.11	0.21	0.67	0.04	Reject H0	1.84	0.14	Reject H0	4.51	0.37	Reject H0

16
17
18 **5.1 Two-Phase Experiment**

19 While the FCFS protocol outperformed traditional signals in every scenario and for every set of buffers, it
20 is important to note that the improvement in intersection performance was affected by the set of buffers
21 used, especially as levels of congestion increased. For the scenario with the lowest level of congestion,
22 the FCFS protocol outperformed the traffic signal by an order of magnitude, with the average delays for
23 the FCFS being under 0.4 seconds for all 3 sets of buffers. In the scenario with the highest level of
24 congestion, the FCFS implementation with the least conservative buffers outperformed the traffic signal
25 by an order of magnitude (0.67 seconds vs. 9.11 seconds), yet the more conservative set of buffers was
26 only able to reduce delay to an average of 4.51 seconds per vehicle. While this is still a significantly
27 improvement over the traditional traffic signal, it is clear that it's affected by the ability of the automated
28 vehicle to sense information, and accurately performing driving actions based on the information. It

1 further shows that determining the appropriate set of buffer is pivotal in proper implementation of the
 2 FCFS protocol.
 3
 4

TABLE 2 Three-phase, protected left turn experiment

Traffic Pattern		Traffic Signals (Y)		FCFS (0.25,0.1,0.25) (X_{25})			FCFS (0.50,0.2,0.50) (X_{50})			FCFS (0.75,0.3,0.75) (X_{75})		
		average delay (s)	sd	average delay (s)	sd	$H_0:Y-X_{25} \leq 0$ $H_A:Y-X_{25} > 0$	average delay (s)	sd	$H_0:Y-X_{50} \leq 0$ $H_A:Y-X_{50} > 0$	average delay (s)	sd	$H_0:Y-X_{75} \leq 0$ $H_A:Y-X_{75} > 0$
Left Turn Volume	Opposite Approach Volume											
200	400	6.59	0.15	0.28	0.02	Reject H_0	0.53	0.03	Reject H_0	0.92	0.06	Reject H_0
200	600	7.45	0.26	0.32	0.03	Reject H_0	0.63	0.03	Reject H_0	1.11	0.07	Reject H_0
200	800	8.84	0.23	0.37	0.02	Reject H_0	0.74	0.04	Reject H_0	1.42	0.07	Reject H_0
200	1000	10.60	0.22	0.41	0.03	Reject H_0	0.90	0.05	Reject H_0	1.77	0.10	Reject H_0
400	400	6.75	0.20	0.33	0.02	Reject H_0	0.61	0.04	Reject H_0	1.10	0.10	Reject H_0
400	600	7.62	0.21	0.36	0.02	Reject H_0	0.71	0.04	Reject H_0	1.35	0.07	Reject H_0
400	800	9.00	0.27	0.42	0.02	Reject H_0	0.90	0.06	Reject H_0	1.63	0.09	Reject H_0
400	1000	10.07	0.23	0.48	0.03	Reject H_0	1.05	0.06	Reject H_0	2.10	0.17	Reject H_0
600	400	7.60	0.34	0.37	0.03	Reject H_0	0.73	0.03	Reject H_0	1.44	0.15	Reject H_0
600	600	8.68	0.24	0.42	0.02	Reject H_0	0.85	0.05	Reject H_0	1.63	0.16	Reject H_0
600	800	10.14	0.45	0.47	0.03	Reject H_0	1.04	0.06	Reject H_0	2.02	0.13	Reject H_0
600	1000	11.00	0.46	0.54	0.03	Reject H_0	1.23	0.09	Reject H_0	2.59	0.14	Reject H_0
800	400	9.73	1.29	0.41	0.03	Reject H_0	0.87	0.06	Reject H_0	2.00	0.28	Reject H_0
800	600	9.88	0.31	0.46	0.03	Reject H_0	1.02	0.08	Reject H_0	2.51	0.60	Reject H_0
800	800	12.53	1.23	0.55	0.04	Reject H_0	1.26	0.10	Reject H_0	3.06	0.46	Reject H_0
800	1000	12.96	0.56	0.63	0.04	Reject H_0	1.50	0.13	Reject H_0	4.20	0.99	Reject H_0
1000	400	13.42	2.54	0.45	0.03	Reject H_0	1.14	0.10	Reject H_0	5.44	2.21	Reject H_0
1000	600	12.08	1.08	0.53	0.03	Reject H_0	1.40	0.14	Reject H_0	6.61	2.03	Reject H_0
1000	800	14.62	1.14	0.61	0.03	Reject H_0	1.63	0.17	Reject H_0	8.86	1.60	Reject H_0
1000	1000	16.06	0.73	0.69	0.04	Reject H_0	1.93	0.19	Reject H_0	9.50	1.95	Reject H_0

5
6

5.2 Three-Phase Experiment

8 While the FCFS implementations again outperform the traffic signal for all scenarios, we once again see
 9 that the improvements seen from the FCFS implementation with more conservative buffers deteriorate
 10 much quicker with increasing flow than with less conservative buffers. Another interesting observation is
 11 that the variation among simulations for the same scenario increased much more significantly in the
 12 presence of increasing left hand turns for the most conservative set of buffers, resulting in a standard
 13 deviation of 1.95 seconds, compared to a standard deviation of 0.37 seconds for the most congested case
 14 in the two-phase experiment.

15 As left turn movements increase the number of conflicts between opposing streams of traffic, it is
 16 expected that varying levels of left turn flows would significantly affect the performance of traditional
 17 signals. As such, it is not surprising to see that left turn volumes are also a significant factor for the
 18 performance of other intersection control systems such as FCFS.

19 An interesting corollary from the results of the 3-phase experiment is that the network flow
 20 distribution in the form of route choice can have a significant impact on the performance of the system
 21 simply by affecting the distribution of left turning movements per intersection: it may be beneficial to
 22 encourage vehicles to distribute left turning vehicles among several intersection when possible.
 23

6. CONCLUSIONS AND FUTURE RESEARCH

25 In this paper, we presented the results of an experimental comparison between a reservation-based
 26 intersection control protocol and an optimized traditional traffic signal, in a population of autonomous
 27 vehicles. The results show that the FCFS protocol performs significantly better than a traditional traffic
 28 signal, reducing average vehicle delay by an order of magnitude in all cases. It was observed, however,
 29 that varying levels of flow affected the observed levels of improvement for different implementations of
 30 FCFS, especially as the safety buffers used by the intersection manager became more conservative. It was

1 further observed that the volume of left turning vehicles would significantly affect the performance of
2 both traditional signals and FCFS.

3 The results are encouraging, and show that further research must be conducted in order to enable
4 deployment of such systems, as well as any other intelligent intersection control system, to exploit the
5 benefits of automated vehicles. If the levels of performance observed in our numerical testing are
6 achievable, the congestion mitigation impacts an intersection management system such as FCFS could
7 have would be enormous. Even the improvements seen from the most conservative set of buffers tested
8 could more than halve the current estimated delay at intersections.

9 While these results are promising, they provide only a starting point for what should be a thriving
10 research field. Several research directions will be taken, not only to further validate the FCFS intersection
11 control strategy, but also to develop more efficient intersection control systems:

12 • While we are confident that similar results will be observed regardless of the intersection
13 configuration, a more thorough set of testing scenarios would not only provide validation, but would also
14 allow for accurate prediction of expected delay reduction that could be achieved by replacing a traditional
15 set of traffic signals with an automated intersection.

16 • While it is important to be able to estimate average vehicle delays at the intersection level, the
17 network level effects of such vehicle reductions are much more significant: improved performance at a
18 single intersection could potentially have a negative overall effect to the network if adjacent intersections
19 are not prepared for the changes in traffic flow patterns and/or flow.

20 • The microsimulator used for testing procedures was custom developed for the testing of
21 automated intersection management techniques. While we are confident that the simulator is realistic,
22 further validation of the simulator results would be desirable using standard commercial packages.
23 Because of the limitations of commercial microsimulation software, the process of validating the AIM4
24 simulator is a complex one, and to our knowledge, there is no trivial validation process.

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